Computational study of simple and water-assisted tautomerism of 1,3-oxazine-4,6-diones and 1,3-thiazine-4,6-diones

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Computational study of simple and water-assisted tautomerism of 1,3-oxazine-4,6-diones and 1,3-thiazine-4,6-diones

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Density functional theory (DFT) calculations are applied to optimise the structure of three possible tautomers of some 5H-1,3-oxazine-4,6-diones and 5H-1,3-thiazine-4,6-diones and their transition states using B3LYP/6-311++G∗∗ level of theory. Then, important molecular parameters, IR frequencies and energetic parameters are calculated. In all cases, tautomer **2** is about 0.7–8.7 kcal/mol more stable than tautomer **1** and about 10.4–14.4 kcal/mol more stable than tautomer **3**. Our results confirm the available experimental data approving the higher stability of tautomer **2**. Furthermore, barrier energies and reaction rate constants of the hydrogen exchange between each pair of tautomers in the presence of one, two and three water molecules are calculated. The computed activation barriers in the presence of water molecules are about 23.8–76.2 kcal/mol lower than those in the gas phase.

Keywords: tautomerism; oxazinedione; thiazinedione; transition state; water assisted

1. Introduction

Oxazinones, thiazinones and their derivatives constitute an important group of heterocycles, which has attracted interest due to their significant role in biological reactions [1]. In recent years, much attention has been focused on the study of these compounds since the discovery of their application in the synthesis of anti-HIV drug [2]. Furthermore, they have shown diverse pharmacological properties such as progesterone receptor antagonist [3], antitumour [4], antiviral [5], antithrombotic [6], antimicrobacterial [7], anti-inflammatory [8], antidiabetic and hypolipidaemic [9] effects. Oxazinones have also been utilised as useful synthetic precursors for the preparation of some organic compounds [10–12] and metal complexes [13].

5H-1,3-Oxazine-4,6-diones (OZDs) and 5H-1,3-thiazine-4,6-diones (TZDs) also have anti-inflammatory and antimicrobacterial activities [14–20]. They can be used in the synthesis of very useful compounds such as α-amino acids [21]. Because of the importance of the title compounds, OZDs and TZDs have been the subject of some studies including the study of their anomeric effect [22], reduction [23], ring contraction [24] and application in DNA chemistry [25].

Since tautomerism in the OZD and TZD structures affects their chemical and biological activities, especially their diverse pharmacological properties [3,7], it is very important to learn about the complete scheme of tautomerism and the reaction path between different tautomers. In this line, the effect of substituents and, more importantly, the effect of solvent on this tautomerism interconversion should also be worked out clearly. Moreover, despite a large number of published reports about the study of tautomerism in different compounds [26–38], the study of tautomerism in OZDs or TZDs has not been reported. Therefore, the relative importance of different tautomers and their interconversion can be studied in detail. Another important feature of these compounds that has not received much attention is the study of intermolecular tautomerism. This type of study is one of the important topics in recent computational reports [39–41].

In this work, structural, bonding and vibrational properties (Tables 5 and 6) and tautomerism in the OZD, TZD, mono- and dimethyl derivatives (Figure 1, **a–h**) and their transition states (Table 2) are studied using DFT-B3LYP/6-311++G∗∗ calculations (Tables 1–4; Figures 3 and 4). Furthermore, the intermolecular tautomerism interconversion and reaction path for one of them (molecule **e**) are also obtained in the presence of one, two and three water molecules (Tables 7 and 8). Details of computations and the results obtained in this work are presented below.

2. Methods

Density functional theory (DFT) has been widely applied by chemists to study the electronic structure of molecules in the past 30 years [42,43]. In this work, all calculations have been carried out at the B3LYP/6-311++ G∗∗ level

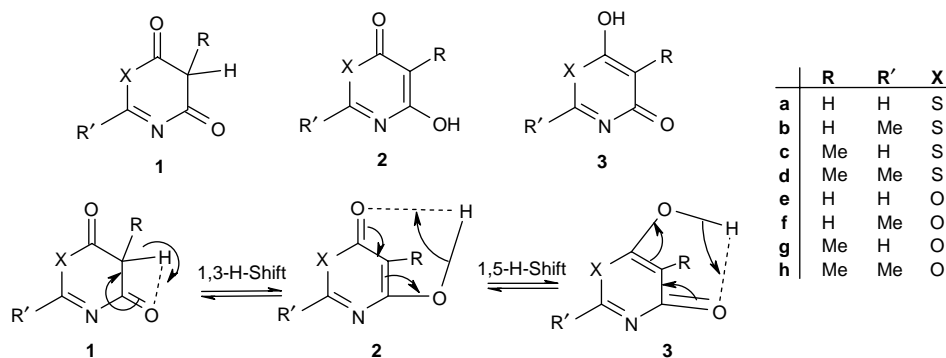*Emails: h_tavakol@uoz.ac.ir; hosein_ta@yahoo.com

Figure 1.   Three possible tautomers of selected compounds with representation of both '1,3' and '1,5' hydrogen shifts.

of theory [44,45]. The B3LYP method has been validated to give results similar to those of the more computationally expensive MP2 theory for molecular geometry and frequency calculations [46,47]. Gaussian 03 [48] and GaussView 03 [49] program packages have been employed for computing and visualising the desired properties. The absence of imaginary frequencies verified that the structures were true minima at their respective levels of theory for each tautomer. Furthermore, in each pair of tautomers, stationary point geometry with one imaginary frequency has been found and the transition state has been identified using Schlegel's synchronous-transit-guided quasi-Newton (QST3) [50,51] method started from the fully optimised structure of one tautomer and finished on the fully optimised structure of another tautomer. Intrinsic reaction coordinate calculations proved that each reactant linked to the correct product via allocated transition state. Calculations of the rate constants and reaction dynamic have been carried out using canonical transition state theory applying the Eyring equation [52–54]. IR frequencies and energies obtained from the frequency calculations were used after applying the appropriate scaling factor (both of them scaled by 0.967; http://cccbdb.nist.gov/vibscalejust.asp). Free energies of solvation for all structures were calculated using SCRF keyword with Tomasi's polarised continuum model (PCM) [55,56] at the B3LYP/6-311++G** level of theory. Four different solvents (cyclohexane, chloroform, acetone and DMSO) with different dielectric constants (respectively, 2.02, 4.90, 20.70 and 46.70) have been used.

3.   Results and discussion

This work was started with eight different structures of OZDs and TZDs. In Figure 1, the structures of all tautomers in eight selected structures are shown. Structures **a**–**d** are TZDs and the other structures (**e**–**h**) are OZDs. According to this figure, three tautomers (**1**–**3**)

can exist for each structure. Spectroscopic data of previous report showed that the major product obtained from the synthesis of some OZDs and TZDs is tautomer **2** [14]. Figure 1 also shows that the interconversions of tautomers **1** to **2** and **1** to **3** are similar to '1,3' hydrogen shift and the interconversion of tautomers **2** to **3** is similar to '1,5' hydrogen shift.

For more simplicity, geometric (*cis–trans* and *syn–anti*) and conformational isomers were neglected in this study. Therefore, only possible tautomers have been considered in the calculations. Concluding, these structures were employed without any symmetry restriction, pre-defined geometric or conformational structures, and *C*1 symmetry was assumed for all structures.

3.1   Optimised structures

Molecular structures of the optimised (final) tautomers and transition states are shown in Tables 1 and 2, respectively.

According to the above tables, optimised structures of tautomers **2** and **3** are completely planar, the structure of tautomer **1** is half-chair or envelope-like with about 15° deviation from the plane, the structure of TS1 (the transition state between tautomers **1** and **2**) is half-chair with about 20° deviation from the plane, the structure of TS2 (the transition state between tautomers **1** and **3**) has a planar ring and slightly spatial ring substituents and the structure of TS3 (the transition state between tautomers **2** and **3**) is completely envelope-like with 36–42° deviation from the plane.

3.2   Molecular parameters

Calculated molecular parameters for optimised structures are listed in Table S1 of the Supplementary Material. The numbering schemes of all molecules are the same as the pre-defined numbers for each atom as shown in Tables 1 and 2. This numbering scheme (Figure 2) can be applied identically for all tautomers and transition states. In Figure 2, only similar numbers of all structures are shown.

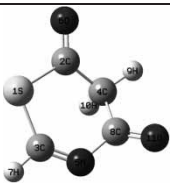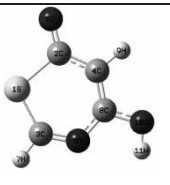Table 1.   Final structure of the optimised tautomers.
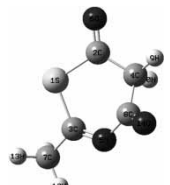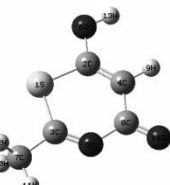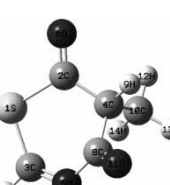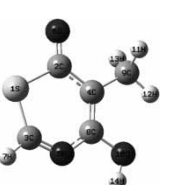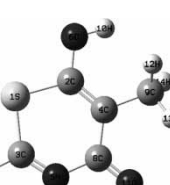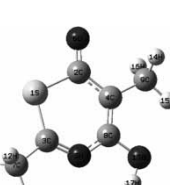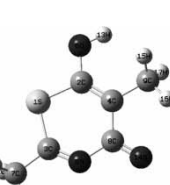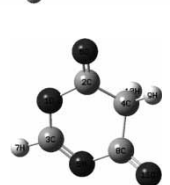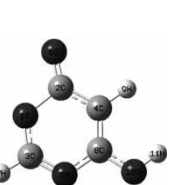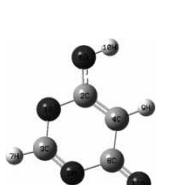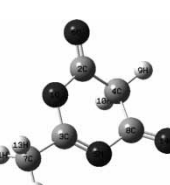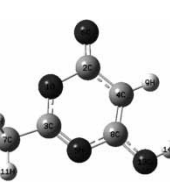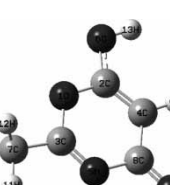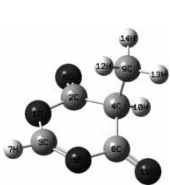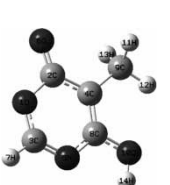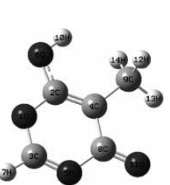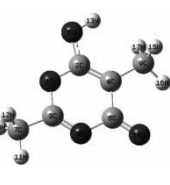
Molecule	Tautomer **1**	Tautomer **2**	Tautomer **3**
a			
b			
c			
d			
e			
f			
g			
h			

Table 2.   Final structure of the optimised transition states.
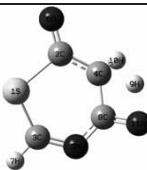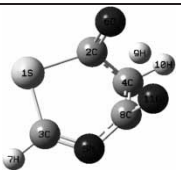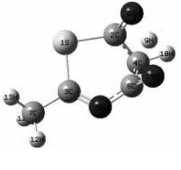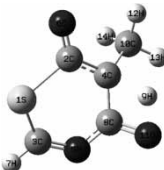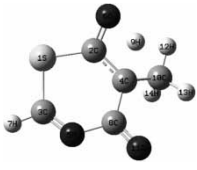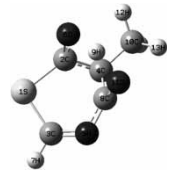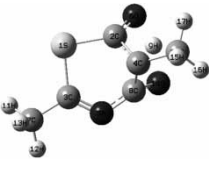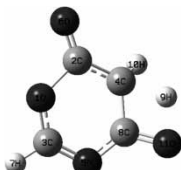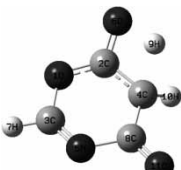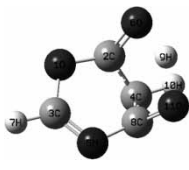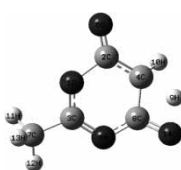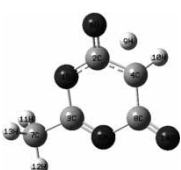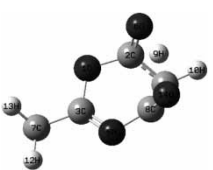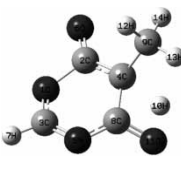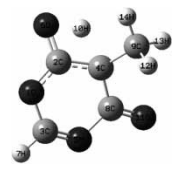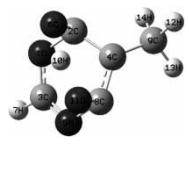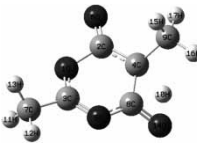
Molecule	TS1 (between tautomers **1** and **2**)	TS2 (between tautomers **1** and **3**)	TS3 (between tautomers **2** and **3**)
a			
b			
c			
d			
e			
f			
g			
h			

Table 3. Kinetic and thermodynamic data of all tautomers and transition states.[a]

Molecule	$\Delta H(1-2)$[b]	$\Delta H(3-2)$[b]	$\Delta G(1-2)$[c]	$\Delta G(3-2)$[c]	$K_{eq}\,(1-2)$[d]	$K_{eq}\,(3-2)$[d]
a	−5.6	−13.7	−5.1	−13.4	5.9×10^3	6.2×10^9
b	−4.6	−13.5	−4.8	−13.0	3.4×10^3	3.1×10^9
c	−8.0	−13.6	−8.7	−13.4	2.2×10^6	6.8×10^9
d	−6.9	−13.4	−8.0	−13.0	6.9×10^5	3.4×10^9
e	−1.6	−10.6	−1.1	−10.4	6.5	4.2×10^7
f	−1.0	−10.9	−0.7	−10.7	3.1	7.0×10^7
g	−8.4	−14.3	−8.6	−14.0	2.1×10^6	2.0×10^{10}
h	−7.8	−14.5	−8.2	−14.4	9.5×10^5	3.4×10^{10}
	$\Delta G^{\#}(2-ts1)$[e]	$\Delta G^{\#}(1-ts2)$[e]	$\Delta G^{\#}(2-ts3)$[e]	$k(2-1)$[f]	$k(1-3)$[f]	$k(2-3)$[f]
a	55.7	62.6	91.3	9.7×10^{-29}	8.7×10^{-34}	7.7×10^{-55}
b	54.9	62.4	91.1	3.3×10^{-28}	1.1×10^{-33}	9.7×10^{-55}
c	60.5	65.2	92.7	2.6×10^{-32}	1.0×10^{-35}	6.8×10^{-56}
d	59.5	65.1	92.3	1.5×10^{-31}	1.1×10^{-35}	1.3×10^{-55}
e	55.1	64.7	93.8	2.4×10^{-28}	2.4×10^{-35}	1.0×10^{-56}
f	54.4	64.8	93.3	8.9×10^{-28}	2.1×10^{-35}	2.6×10^{-56}
g	71.6	66.6	98.4	2.1×10^{-40}	1.0×10^{-36}	4.9×10^{-60}
h	63.2	66.6	97.9	3.0×10^{-34}	9.1×10^{-37}	1.1×10^{-59}

Note: The reference for all differences is the most stable compound.[a] All ΔH and ΔG values were reported in kcal/mol and rate constants were reported in s^{-1}. [b] $\Delta H(n-m)$ = Enthalpy of tautomer $m(Hm)$ − Enthalpy of tautomer $n(Hn)$. [c] $\Delta G(n-m)$ = Gibbs free energy of tautomer $m(Gm)$ − Gibbs free energy of tautomer $n(Gn)$. [d] $K_{eq}(n-m)$: the ratio of $[m]/[n]$, obtained from $K_{eq} = \exp(-\Delta G(n-m)/RT)$. [e] $\Delta G^{\#}(n-ts1)$ = Gibbs free energy of ts1 $(Gts1)$ − Gibbs free energy of tautomer $n(Gn)$. [f] $k(n-m)$: the reaction rate for conversion of n to m.

The X_1—C_2 bond lengths in molecules **a**–**d** lie between 1.7 and 1.9 Å. Its length is exactly 1.8 Å in tautomers **1** and **3**, and TS3, 1.9 Å in tautomer **2** and TS1 and 1.7 Å in TS2 in all optimised TZDs. In addition, its length is 1.4 Å in tautomers **1** and **2** and TS3, 1.3 Å in tautomer **3** and TS2, and 1.5 Å in TS1 in calculated OZDs. Higher atomic radius of sulphur vs. oxygen is responsible for the greater value of the X_1—C_2 bond length in molecules **a**–**d**. The bond lengths of C_3—N_5 and C_3—H_7 (or C_3—C_7) in OZDs have the same value as those in TZDs. In addition, the length of the C_2—O_6 bond lies between 1.2 and 1.4 Å, and the C_4—C_8 bond length lies between 1.4 and 1.5 Å.

Observing bond angle variations, hybridisation changes in the central atom of each angle can be followed. In molecules **a**–**d**, C_2—X_1—C_3 bond angles in tautomers **1** and **2**, and TS1 are more than 100°, and those in TS2, and TS3 and tautomer **3** are less than 100°. C_2—X_1—C_3 and X_1—C_2—C_4 angles in mol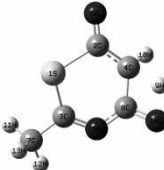ecules **e**–**h** are in general larger than those in molecules **a**–**d**. X_1—C_2—O_6, C_4—C_2—O_6 and X_1—C_3—N_5 angles have expected values according to the hybridisation of their central atom.

The planarity of molecules can be followed by dihedral angles. For example, in tautomers **2** and **3**, C_3—X_1—C_2—C_4, C_2—X_1—C_3—N_5 and X_1—C_2—C_4—C_8 dihedral angles are near 0° and C_3—X_1—C_2—O_6 and C_2—X_1—C_3—H_7 dihedral angles are near 180°, thus all of these angles confirm the planarity of the corresponding tautomers. Following this, in all structures, the value of the deviation of this dihedral angle from 0° (or 180°) is a criterion of the deviation rate from the planar structure.

3.3 Kinetic and thermodynamic data

In Table 3, Gibbs free energies and other important thermodynamic and kinetic data for all structures at 298.15 K and 1 atmosphere pressure are presented. All equilibrium constants for tautomeric interconversion were calculated using $\Delta G = -RT \ln K_{eq}$.

The data presented in Table 3 show that tautomer **2** is most stable, followed by tautomer **1**, and tautomer **3** is least stable in all computed OZDs and TZDs. The difference between Gibbs free energies for tautomers **1** and **2** (Gibbs free energy of tautomer **2** (the most stable tautomer) minus Gibbs free energy of tautomer **1**) lies between −0.7 and −8.7 kcal/mol and for tautomers **3** and **2** (Gibbs free energy of tautomer **2** (the most stable tautomer) minus Gibbs free energy of tautomer **3**) lies between −10.4 and −14.4 kcal/mol. The differences between tautomers **1** and **2** in molecules **e** and **f** are smaller than those in the other molecules. This observation can be the subject of further investigation. Moreover, the value of the equilibrium constant (obtained from Gibbs free energies) for the conversion of tautomer **1** to **2** (the most stable tautomer) lies between 3.1 and 2.2×10^6 and the equilibrium constant for the conversion of tautomer **3** to **2** (the most stable tautomer) lies between 4.2×10^7 and 3.4×10^{10}.

The effects of the substituent were also studied. The thermodynamic results show that the addition of the methyl substituent at the C4 position (between two carbonyl groups) causes the increase in the relative stability of tautomer **2** vs. **1** because the absolute values of ΔG between these two tautomers in molecules **c**, **d**, **g** and **h** (i.e. all of them have methyl at C4) were increased. This phenomenon

Table 4.   Solvation effects with kinetic and thermodynamic data in solvent for all molecules at B3LYP/6-311++G** level of theory.[a]

Solvent	Molecules	a	b	c	d	e	f	g	h
ΔG solvation in acetone	Tautomer **1**	−5.4	−5.5	−4.3	−4.3	−5.9	−6.2	−4.8	−5.0
	Tautomer **2**	−5.0	−5.0	−4.5	−4.5	−7.4	−7.1	−4.9	−4.9
	Tautomer **3**	−8.5	−8.3	−6.8	−6.5	−8.9	−8.8	−7.1	−7.5
	TS1	−4.6	−4.6	−3.4	−3.3	−4.9	−5.0	−3.7	−4.1
	TS2	−6.2	−5.3	−5.1	−4.8	−5.8	−5.8	−5.2	−5.2
	TS3	−2.8	−3.0	−2.9	−2.9	−2.9	−3.2	−2.8	−3.0
ΔG solvation in cyclohexane	Tautomer **1**	−3.4	−3.5	−2.8	−2.7	−3.3	−3.5	−2.7	−2.8
	Tautomer **2**	−3.5	−3.5	−3.4	−3.4	−3.9	−4.0	−3.1	−3.3
	Tautomer **3**	−4.8	−4.8	−4.2	−4.3	−4.6	−4.7	−3.9	−4.2
	TS1	−3.2	−3.4	−2.6	−2.6	−3.0	−3.2	−2.4	−2.7
	TS2	−3.9	−3.4	−3.3	−3.3	−3.3	−3.5	−3.0	−3.1
	TS3	−2.3	−2.8	−2.7	−2.7	−2.2	−2.5	−2.5	−2.6
ΔG solvation in chloroform	Tautomer **1**	−3.4	−3.4	−2.4	−2.2	−3.8	−3.9	−2.8	−2.8
	Tautomer **2**	−3.2	−3.0	−2.6	−2.4	−4.8	−4.5	−2.8	−2.7
	Tautomer **3**	−5.7	−5.4	−4.2	−3.9	−6.0	−5.7	−4.5	−4.5
	TS1	−2.8	−2.7	−1.6	−1.4	−3.0	−2.9	−2.1	−2.0
	TS2	−4.0	−3.1	−2.9	−2.5	−3.6	−3.5	−2.9	−2.8
	TS3	−1.6	−1.5	−1.4	−1.3	−1.7	−1.6	−1.4	−1.3
ΔG solvation in DMSO	Tautomer **1**	−5.0	−5.0	−3.6	−3.4	−5.5	−5.7	−4.1	−4.2
	Tautomer **2**	−4.7	−4.4	−4.0	−3.8	−7.1	−6.7	−4.3	−4.2
	Tautomer **3**	−8.3	−7.9	−6.4	−5.9	−8.7	−8.4	−6.7	−6.9
	TS1	−4.2	−4.0	−2.7	−2.4	−4.5	−4.4	−3.0	−3.3
	TS2	−5.9	−4.3	−4.5	−4.0	−5.4	−5.3	−4.6	−4.4
	TS3	−2.5	−2.4	−2.3	−2.2	−2.4	−2.6	−2.3	−2.3
Thermodynamic and kinetic data in solvent									
Acetone	$K_{eq}(1-2)$[b]	3.1×10^3	1.3×10^3	3.2×10^6	9.9×10^5	7.5×10^1	1.4×10^1	2.4×10^6	7.4×10^5
	$K_{eq}(3-2)$[b]	1.7×10^7	1.2×10^7	1.4×10^8	1.1×10^8	3.0×10^6	4.2×10^6	4.4×10^8	4.4×10^8
	$k(2-1)$[c]	4.7×10^{-29}	1.8×10^{-28}	4.2×10^{-33}	2.0×10^{-32}	3.8×10^{-30}	2.6×10^{-29}	2.9×10^{-41}	8.6×10^{-35}
	$k(1-3)$[c]	3.3×10^{-33}	7.8×10^{-34}	4.5×10^{-35}	2.7×10^{-35}	2.0×10^{-35}	1.0×10^{-35}	2.1×10^{-36}	1.1×10^{-36}
	$k(2-3)$[c]	1.8×10^{-56}	3.5×10^{-56}	4.9×10^{-57}	1.0×10^{-56}	5.4×10^{-60}	3.5×10^{-59}	1.5×10^{-61}	4.5×10^{-61}
Cyclohexane	$K_{eq}(1-2)$[b]	6.8×10^3	3.4×10^3	6.0×10^6	2.3×10^6	1.9×10^1	7.2	4.2×10^6	1.9×10^6
	$K_{eq}(3-2)$[b]	6.7×10^8	3.6×10^8	1.6×10^9	8.6×10^8	1.3×10^7	2.3×10^7	4.6×10^9	7.7×10^9
	$k(2-1)$[c]	6.3×10^{-29}	2.5×10^{-28}	6.7×10^{-32}	3.7×10^{-32}	5.2×10^{-29}	2.3×10^{-28}	6.8×10^{-41}	1.2×10^{-34}
	$k(1-3)$[c]	2.1×10^{-33}	9.1×10^{-34}	2.6×10^{-35}	2.9×10^{-35}	2.7×10^{-35}	2.2×10^{-35}	1.7×10^{-36}	1.5×10^{-36}
	$k(2-3)$[c]	1.1×10^{-55}	2.6×10^{-55}	2.1×10^{-56}	4.2×10^{-56}	6.3×10^{-58}	2.0×10^{-57}	1.8×10^{-60}	3.3×10^{-60}
Chloroform	$K_{eq}(1-2)$[b]	3.8×10^3	1.6×10^3	3.0×10^6	1.0×10^6	3.5×10^1	8.8	2.2×10^6	8.4×10^5
	$K_{eq}(3-2)$[b]	8.0×10^7	5.0×10^7	4.3×10^8	2.9×10^8	5.5×10^6	8.7×10^6	1.3×10^9	1.7×10^9
	$k(2-1)$[c]	5.5×10^{-29}	2.0×10^{-28}	5.2×10^{-33}	2.6×10^{-32}	1.2×10^{-29}	6.2×10^{-29}	5.7×10^{-41}	8.9×10^{-35}
	$k(1-3)$[c]	2.3×10^{-33}	6.9×10^{-34}	2.5×10^{-35}	2.0×10^{-35}	1.7×10^{-35}	1.1×10^{-35}	1.2×10^{-36}	9.1×10^{-37}
	$k(2-3)$[c]	5.6×10^{-56}	9.0×10^{-56}	1.0×10^{-56}	2.0×10^{-56}	5.2×10^{-59}	2.1×10^{-58}	4.3×10^{-61}	1.1×10^{-60}
DMSO	$K_{eq}(1-2)$[b]	3.2×10^3	1.4×10^3	4.2×10^6	1.3×10^6	9.0×10^1	1.6×10^1	2.9×10^6	9.0×10^5
	$K_{eq}(3-2)$[b]	1.3×10^7	8.6×10^6	1.2×10^8	9.2×10^7	2.6×10^6	3.7×10^6	3.6×10^8	3.4×10^8
	$k(2-1)$[c]	4.4×10^{-29}	1.6×10^{-28}	3.0×10^{-33}	1.4×10^{-32}	2.9×10^{-30}	2.0×10^{-29}	2.2×10^{-41}	6.6×10^{-35}
	$k(1-3)$[c]	3.7×10^{-33}	3.6×10^{-34}	5.0×10^{-35}	3.0×10^{-35}	1.9×10^{-35}	1.1×10^{-35}	2.1×10^{-36}	1.3×10^{-36}
	$k(2-3)$[c]	2.1×10^{-56}	3.3×10^{-56}	4.4×10^{-57}	8.8×10^{-57}	3.9×10^{-60}	2.6×10^{-59}	1.4×10^{-61}	4.2×10^{-61}

Notes: [a]All energetic data have been reported in kcal/mol. [b]$K_{eq}(n - m)$: the ratio of $[m]/[n]$, obtained from $K_{eq} = \exp(-\Delta G(n - m)/RT)$. [c]$k(n - m)$: the reaction rate for conversion of n to m.
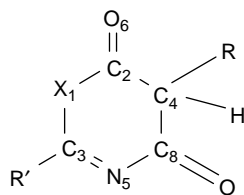
Figure 2. Numbering scheme for all tautomers and transition states.

was observed due to unfavourable spatial interaction at sp^3 carbon (C4) of tautomer **1** while in tautomer **2**, this carbon has sp^2 hybridisation and a planar structure. Moreover, all rate constants in these four molecules are smaller than those in the other molecules (**a**, **b**, **e** and **f**) that did not have the methyl substituent at the C4 position.

Rate constants of these conversions (obtained from barrier energies) are shown in the second part of Table 3. The barrier energies ($\Delta G^\#$) for the interconversion of tautomers are high and, following this, the corresponding reactions are carried out very slowly at room temperature. The difference between Gibbs free energies for TS1 and tautomer **2** ($\Delta G^\#(2 - ts1)$) lies between 54.9 and 71.6 kcal/mol, for TS2 and tautomer **1** ($\Delta G^\#(1 - ts2)$) lies between 62.4 and 66.6 kcal/mol and for TS3 and tautomer **2** ($\Delta G^\#(2 - ts3)$) lies between 91.1 and 98.4 kcal/mol. Therefore, all rate constants for the interconversion of tautomers are very low at room temperature. These data confirmed that, in both '1,3' and '1,5' hydrogen shifts, because of high energy barriers, the interconversion of tautomers is very slow at room temperature without using a catalyst or solvent assistance.

3.4 Solvation effect

Four different solvents (acetone, cyclohexane, chloroform and DMSO) with different dipole moments were

used for computing free energies of solvation. Only aprotic solvents were employed in this part of study, so that the effects of protic solvents such as water were not considered, and the solvent-assisted tautomerism in the presence of water (as the protic solvent) will be discussed in Section 3.6. The results of these calculations are presented in Table 4. PCM calculations provide the total free energies of solvation, so the Gibbs free energies of compounds in the solvent can be obtained by this method.

As it is shown in Table 4, ΔG solvation for all optimised tautomers and transition states are negative and their values lie between -1.3 and -8.9 kcal/mol. These values were applied to calculate final ΔG between tautomers, $\Delta G^\#$ between each tautomer and the related transition state, and the rate and equilibrium constants of tautomerism in each solvent. For example, the maximum rate constant of tautomerism interconversion in all four solvents is $2.3 \times 10^{-28}\,\text{s}^{-1}$ and the maximum rate constant in the gas phase is $8.9 \times 10^{-28}\,\text{s}^{-1}$. Furthermore, in different solvents, the equilibrium constant between tautomers **1** and **2** ($K_{eq}(1 - 2)$) lies between 8.8 and 6.0×10^6 kcal/mol and between tautomers **2** and **3** ($K_{eq}(2 - 3)$) lies between 1.3×10^{-10} and 3.8×10^{-7} kcal/mol. Since the effect of the solvent on the stability of each structure (tautomer or transition state) is different, all equilibrium constants in solvents are different from those in the gas phase.

The diagram for the variation of ΔG solvation in each solvent vs. structures is shown in Figure 3 and the variation of ΔG solvation of each tautomer or transition state vs. solvents is shown in Figure 4. By observing Figure 3, it is easily seen that the order of the absolute amount of ΔG solvation is found to be acetone > DMSO > cyclohexane > chloroform. From Figure 4, tautomer **3** has the maximum absolute amount in ΔG solvation and
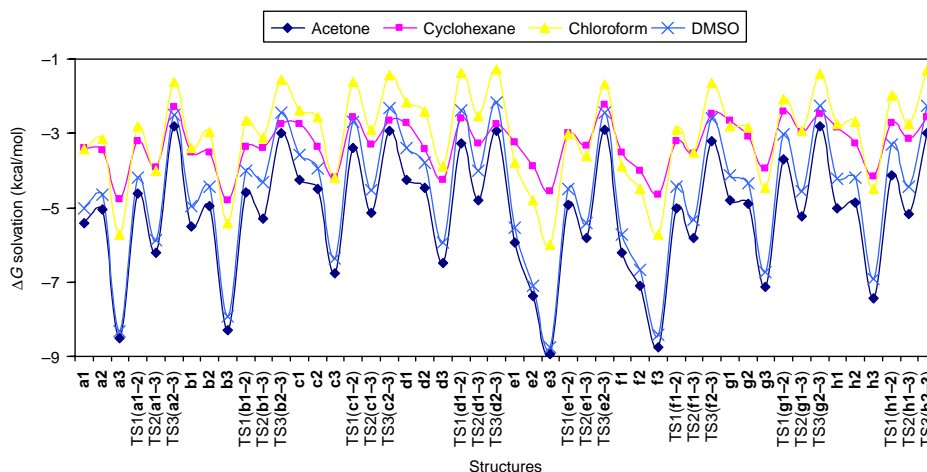

Figure 3. Variation of ΔG solvation in each solvent vs. all structures.
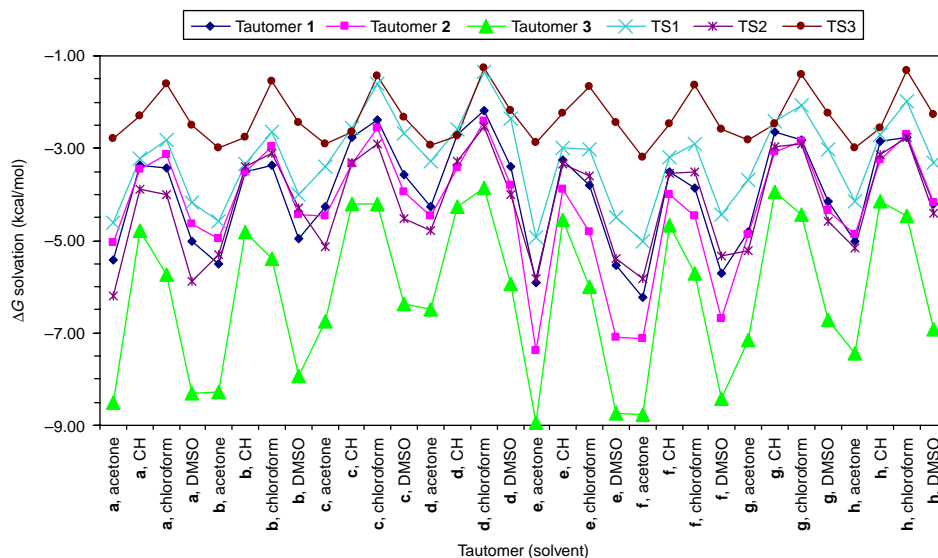
Figure 4.　Variation of ΔG solvation in each tautomer or transition states. CH, cyclohexane.

TS3 and then TS2 have the minimum absolute amounts in ΔG solvation. The results of our PCM calculations show that this tautomerism interconversion is not effected extensively by the solvent. In other words, the equilibrium and rate constant in four different solvents (with different dipole moments) are comparable with those in the gas phase. This interconversion is very slow in both the gas phase and solvent.

3.5　Frequencies

In Table 5, some calculated frequencies of optimised structures are reported after correction by the scaling factor (see Section 2). The first column of Table 5 consists of C=O frequencies. In all structures except TS3, the value of this frequency is about $1700\,cm^{-1}$. In TS3, the order of the CO bond is between 1 and 2 and the frequency between 1387 and $1476\,cm^{-1}$ is normal for this bond. C=N, C=C

Table 5.　Most important frequencies (in cm^{-1}) of all structures.

Molecule	C=O	C=N	C=C	O—H	Molecule	C=O	C=N	C=C	O—H
a1	1747	1568	–	–	**e1**	1814	1602	–	–
a2	1708	1501	1588	3626	**e2**	1779	1535	1593	3669
a3	1670	1534	1600	3640.8	**e3**	1700	1564	1653	3675
TS1(**a1**−**2**)	1756	1484	1508	1825	TS1(**e1**−**2**)	1831	1532	1514	1802
TS2(**a1**−**3**)	1708	1589	1436	1746	TS2(**e1**−**3**)	1733	1631	1536	1779
TS3(**a2**−**3**)	1449	1541	1397	1747	TS3(**e2**−**3**)	1476	1582	1438	1745
b1	1741	1598	–	–	**f1**	1806	1620	–	–
b2	1703	1520	1591	3628	**f2**	1772	1594	1546	3671
b3	1669	1546	1616	3643	**f3**	1700	1662	1579	3676
TS1(**b1**−**2**)	1749	1523	1491	1829	TS1(**f1**−**2**)	1821	1542	1514	1806
TS2(**b1**−**3**)	1708	1622	1429	1754	TS2(**f1**−**3**)	1733	1659	1529	1783
TS3(**b2**−**3**)	1447	1581	1390	1754	TS3(**f2**−**3**)	1470	1624	1432	1748
c1	1738	1568	–	–	**g1**	1806	1601	–	–
c2	1676	1512	1586	3633	**g2**	1762	1551	1627	3638
c3	1654	1538	1591	3646	**g3**	1684	1571	1649	3674
TS1(**c1**−**2**)	1732	1508	1473	1834	TS1(**g1**−**2**)	1806	1540	1483	1752
TS2(**c1**−**3**)	1692	1584	1417	1766	TS2(**g1**−**3**)	1713	1626	1517	1787
TS3(**c2**−**3**)	1416	1542	1391	1753	TS3(**g2**−**3**)	1466	1583	1415	1748
d1	1732	1597	–	–	**h1**	1798	1618	–	–
d2	1673	1531	1592	3632	**h2**	1756	1564	1627	3637
d3	1656	1606	1551	3647	**h3**	1689	1589	1652	3674
TS1(**d1**−**2**)	1726	1531	1477	1838	TS1(**h1**−**2**)	1794	1551	1496	1812
TS2(**d1**−**3**)	1696	1615	1410	1773	TS2(**h1**−**3**)	1716	1650	1509	1789
TS3(**d2**−**3**)	1387	1580	1300	1756	TS3(**h2**−**3**)	1463	1625	1412	1750

Note: All frequencies have been reported after correction by the scaling factor.

Table 6.   Comparison between computational and experimental IR frequencies (in cm^{-1}).

	Average of computed frequencies	Average of this frequency for reference compounds	% Error
X=S			
C=O	1707	1618	5.2
C=N	1555	1582	1.7
O—H	3422	3188	6.9
X=O			
C=O	1761	1741	1.1
C=N	1592	1610	1.1
O—H	3452	3220	6.7

and O—H frequencies are reported, respectively, in the second, third and fourth columns of Table 5.

All of these calculated frequencies are in accordance with the same frequency in similar compounds. To prove this claim, calculated frequencies have been compared with experimental frequencies (extracted from [14]) and the results are shown in Table 6. The data reported in this table show that our computational frequencies are comparable with experimental frequencies and the maximum value of calculation error is 6.9%. These frequency data and their comparisons with the experiments show the potency of our method to use it instead of experiment (which will be more expensive) for the determination of molecular and spectral parameters. Hence, IR calculations were used for the cross-validation of the calculated tautomers with the experiments.

Table 7.   Final structure of optimised tautomers and transition states in the presence of one, two and three water molecules.
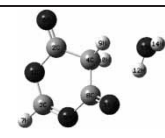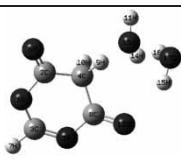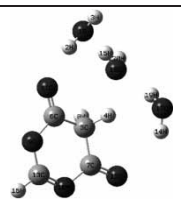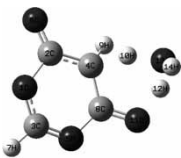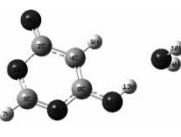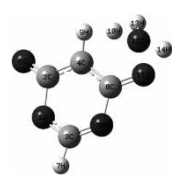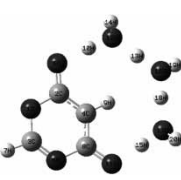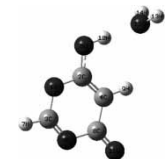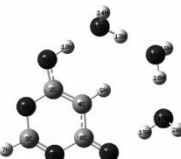
Molecule	One water molecule	Two water molecules	Three water molecules
e1			
TS1(**e1**–**2**)			
e2			
TS2(**e2**–**3**)			
e3			

Table 8. Corrected kinetic and thermodynamic data of molecule **1** in the presence of one, two and three water molecules at B3LYP/6-311++G** level of theory[a].

Number of water molecules	$\Delta H(1-2)$[b]	$\Delta H(3-2)$[b]	$\Delta G(1-2)$[c]	$\Delta G(3-2)$[c]	$K_{eq}(1-2)$[d]	$K_{eq}(3-2)$[d]	$\Delta G^{\#}(2-ts1)$[e]	$\Delta G^{\#}(2-ts3)$[e]	$k(2-1)$[f]	$k(2-3)$[f]
0	−1.6	−10.6	−1.1	−10.4	6.5	4.2×10^7	55.1	93.8	2.4×10^{-28}	1.0×10^{-56}
1	−5.1	−9.6	−4.9	−9.3	3.8×10^3	6.6×10^6	32.9	34.5	4.5×10^{-12}	3.2×10^{-13}
2	−11.1	−7.2	−7.8	−7.6	4.9×10^5	3.6×10^5	23.8	20.2	2.2×10^{-5}	1.0×10^{-2}
3	−15.1	−6.6	−14.6	−6.9	5.1×10^{10}	1.2×10^5	21.2	17.6	1.8×10^{-3}	7.3×10^{-1}

Notes: [a]All ΔH and ΔG values were reported in kcal/mol and rate constants were reported in s^{-1}. [b] $\Delta H(n-m)$ = Enthalpy of tautomer $m(Hm)$ − Enthalpy of tautomer $n(Hn)$. [c] $\Delta G(n-m)$ = Gibbs free energy of tautomer $m(Gm)$ − Gibbs free energy of tautomer $n(Gn)$. [d] $K_{eq}(n-m)$ = equilibrium constant of tautomer $n(Gn)$. [e] $\Delta G^{\#}(n-ts1)$ = Gibbs free energy of ts1 (Gts1) − Gibbs free energy of tautomer $n(Gn)$. [f] $k(n-m)$: the reaction rate for conversion of n to m.

$K_{eq} = \exp(-\Delta G(n-m)/RT)$, obtained from $K_{eq} = [m]/[n]$, the ratio of $[m]/[n]$: the ratio of tautomer $n(Gn)$.

3.6   *Water-assisted tautomerism*

Intermolecular tautomerism of molecule **e** in the presence of one, two and three water molecules was studied at the B3LYP/6-311++G** level of theory. The optimised structures are shown in Table 7 and kinetic and thermodynamic results of these calculations are listed in Table 8.

The data reported in Table 8 show that the values of $\Delta G(1-2)$ for molecule **e** are -1.1, -4.9, -7.8 and -14.6 kcal/mol, respectively, in the gas phase and with one, two and three water molecules. These data show that the effect of water molecules on the stability of tautomer **2** is more than that for tautomer **1**. Moreover, $\Delta G(3-2)$ values are -10.4, -9.3, -7.6 and -6.9 kcal/mol, respectively, in the gas phase and with one, two and three water molecules.

The kinetic effects of water-assisted tautomerism are more profound than thermodynamic effects. All water-assisted tautomerism rate constants are higher than simple tautomerism rate constants. For example, the rate constant for the conversion of **e2** to **e1** ($k(2-1)$) from 2.4×10^{-28} in the absence of water (in the gas phase) goes up to 4.5×10^{-12}, 2.2×10^{-5} and 1.8×10^{-3}, respectively, with one, two and three water molecules. In addition, the rate constant for the conversion of **e2** to **e3** ($k(2-3)$) from 1.0×10^{-56} in the absence of water (in the gas phase) goes up to 3.2×10^{-13}, 1.0×10^{-2} and 7.3×10^{-1}, respectively, with one, two and three water molecules. Finally, activation barriers in the presence of water molecules are in general lower than those in the gas phase.

4.   Conclusion

In this work, DFT calculations have been applied to the study of structures, molecular parameters and vibrational frequencies of three possible tautomers of some OZDs and TZDs using the B3LYP/6-311++G** level of theory. Calculated frequencies show good agreement with the experiment. Moreover, kinetic and thermodynamic behaviour of these tautomeric interconversions in the gas phase have been studied. In all structures, tautomer **2** is most stable and tautomer **3** is least stable. Optimisation of structures in four different solvents (acetone, chloroform, DMSO and cyclohexane) has been investigated and the results show a little difference between the gas and solvent calculations. In addition, the tautomerism interconversion in the presence of one, two and three water molecules has been studied. The results show that, although the simple interconversion of tautomers is very slow, it can be done faster in the presence of water molecules. All reaction rate constants are increased by increasing the number of water molecules near the tautomers.

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